

# 25 –Mavzu

Differensiyal hisob asosiy  
teoremlari

# 1 Aniqmasliklarni ochish

## Lopital qoidalari

Teorema (Lopital) .Biror  $a \in \mathbb{R}$  nuqta atrofida  $f(x), g(x)$  aniqlanib, hosilalar mavjud bo'lsin.  $\lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow a} g(x) = 0, g'(x) \neq 0$  .U holda, agar

$\lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$  mavjud bo'lsa,  $\lim_{x \rightarrow a} \frac{f(x)}{g(x)}$  ham mavjud va  $\lim_{x \rightarrow a} \frac{f(x)}{g(x)} = \lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$

# 2 Teylor formulasi

Teorema (Teylor Bruk):  $f(x)$  funksiya  $c$  nuqta va uning atrofida  $(n+1)$ - tartibli hosilaga ega bo'lsin.  $c$  va  $x$  orasida shunday  $\xi$  nuqta mavjudki, quyidagi formula o'rinli.

$$f(x) = f(c) + \frac{f'(c)}{1!}(x-c) + \frac{f''(c)}{2!}(x-c)^2 + \dots + \frac{f^{(n)}(c)}{n!}(x-c)^n + \frac{f^{(n+1)}(\xi)}{(n+1)!}(x-c)^{n+1}$$

Agar Teylor formulasida  $c=0$  bo'lsa Makloren K. formulasi

$$f(x) = f(0) + \frac{f'(0)}{1!}x + \frac{f''(0)}{2!}x^2 + \dots + \frac{f^{(n)}(0)}{n!}x^n + R_{n+1}(x)$$

hosil bo'ladi.

Makloren formulasi bo'yicha quyidagi yoyilmalarni olish mumkin

$$1. e^x = 1 + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots + \frac{x^n}{n!} + o(x^n),$$

$$2. \sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots + (-1)^{n-1} \frac{x^{2n-1}}{(2n-1)!} + o(x^{2n}),$$

$$3. \cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots + (-1)^n \frac{x^{2n}}{(2n)!} + o(x^{2n+1}),$$

$$4. (1+x)^m = 1 + mx + \frac{m(m-1)}{2!} x^2 + \dots + \frac{m(m-1)\dots(m-n+1)}{n!} x^n + o(x^n),$$

$$5. \ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \dots + (-1)^{n-1} \frac{x^n}{n} + o(x^n).$$

Misollar. 1)  $f(x) = \sqrt{x}$  funksiyani  $x-1$  darajalari bo'yicha yoyilmasi uchta hadini toping.

Taylor formulasi bo'yicha

$$f(x) = f(1) + \frac{f'(1)}{1!} (x-1) + \frac{f''(1)}{2!} (x-1)^2 + \dots$$

$f'(x) = \frac{1}{2\sqrt{x}}, f''(x) = -\frac{1}{4\sqrt{x^3}}$

Demak, 
$$\sqrt{x} = 1 + \frac{1}{2}(x-1) - \frac{1}{8}(x-1)^2 + 0((x-1)^2).$$