



**NATIONAL UNIVERSITY OF UZBEKISTAN
SAMARKAND STATE UNIVERSITY
V.I. ROMANOVSKIY INSTITUTE OF MATHEMATICS
NATURAL SCIENCE PUBLISHING**

ABSTRACTS

OF VIII INTERNATIONAL SCIENTIFIC CONFERENCE

ACTUAL PROBLEMS OF APPLIED MATHEMATICS AND INFORMATION TECHNOLOGIES-AL-KHWARIZMI 2023

Dedicated to the 105th anniversary of the National University of Uzbekistan and the 1240th anniversary of Musa Al-Khwarizmi

**SamSU, SAMARKAND - UZBEKISTAN,
SEPTEMBER 25–26, 2023**

<https://apmath.nuu.uz>

**The National University of Uzbekistan
named after Mirzo Ulugbek**

V.I. Romanovskii institute of mathematics

**Samarkand state university
named after Sharof Rashidov**

Natural Science publishing

ABSTRACTS

**OF THE 8TH INTERNATIONAL CONFERENCE
“ACTUAL PROBLEMS OF APPLIED
MATHEMATICS AND INFORMATION
TECHNOLOGIES” - AL-KHWARIZMI 2023**

September 25-26, 2023

SamSU, Samarkand, Uzbekistan

On some spaces of the space of complete linked systems that are manifolds of infinite dimension

Zhuraev T. F.¹, Tursunova Z. O.¹, Zhuvonov Q. R.²

¹Tashkent State Pedagogical University named after Nizami, Tashkent, Uzbekistan,
tursunzhuraev@mail.ru, tu-zulya@mail.ru;

²“TIIAME”, National Research University. Tashkent. Uzbekistan,
qamariddin.j@mail.ru

In this paper, topological and geometric properties of the set of complete linked systems are considered.

A linked system ξ of closed subsets of a space is called maximal if it has the following property:

“if the closed set $A \subset X$ intersects every element of ξ ”, then $A \in \xi$ [1]. (*) A linked system ξ of closed subsets is said to be complete [2] if the following condition is true for any closed set $F \subset X$:

“any neighborhood OF of F contains $\Phi \in \xi$ ” implies $\Phi \in \xi$ [2].(**)

A system of closed subsets $\mu = \{F_\alpha : F_\alpha \subset X; \alpha \in A\}$ of the space X is called a k -linked ($k \geq 2$) if the intersection of any k -elements of the μ system is non-empty. those. $\forall \alpha_1, \alpha_2, \dots, \alpha_k, F_{\alpha_i} \in \mu, \alpha_i \in A \Rightarrow \bigcap_{i=1}^k F_{\alpha_i} \neq \emptyset$.

Denote by $N_k(X)$ the set of all complete k -linked systems (for short, n_{kcc}) of the space X . Therefore, for any natural number $n \in N$ one can define a subspace $N^n(X)$ of the space $N(X)$ consisting of all ncc whose support consists of at most points. those. $N^n(X) = \{\xi \in N(X) : |supp\xi| \leq n\}$.

For a compact X , by $\lambda_\omega(X)$, $N_\omega(X)$, and $N^\omega(X)$ we denote, respectively, the subsets of $\bigcup_{n=1}^\infty \lambda_n(X)$, $\bigcup_{K=1}^\infty N_K(X)$ and $\bigcup_{n=1}^\infty N^n(X)$.

A set $B(Q)$ is called a boundary set in Q if $Q \setminus B(Q) \approx \ell_2$ [3], a topological space X is called a manifold modeled on the space Y or a Y manifold, if every point in space X has a neighborhood homeomorphic to an open subset of space Y .

The following results are obtained:

Theorem 1. For any metrizable nondegenerate continuum X , the following holds:

- a) $\lambda_\omega(X)$ is the boundary set of $\lambda(X)$;
- b) $N_\omega(X)$ is the boundary set of $N(X)$;
- c) $N^\omega(X)$ is the boundary set of $K\lambda(X)$.

Theorem 2. For any metrizable non-degenerate continuum X we have:

- a) $N(X) \setminus N_n(X)$ is a Q manifold, for any $n \geq 2$;
- b) $\lambda(X) \setminus \lambda_n(X)$ is a Q manifold, for any $n \geq 2$;
- c) $N(X) \setminus N^n(X)$ is a Q manifold, for any $n \geq 2$.

References

1. J. Van Mill Superextensions of metrizable continua are Hilbert cubes // Fund.Math 1980 v. 107. p. 204-218.
2. A. B. Ivanov On the space of complete linked systems // Sib.mat.zhurnal 1986, Vol. 27.6, p. 95 – 110.
3. T.Banakh, T.Radul, M.Zarichny, Absorbing sets in infinite – dimensional Manifolds // Math. Studies Monogh., Ser. V.1, VNTL Publishers, 1996, p. 232.

**The National University of Uzbekistan
named after Mirzo Ulugbek**

V.I. Romanovskii institute of mathematics

**Samarkand state university
named after Sharof Rashidov**

Natural Science publishing

ABSTRACTS

**OF THE 8TH INTERNATIONAL CONFERENCE
“ACTUAL PROBLEMS OF APPLIED
MATHEMATICS AND INFORMATION
TECHNOLOGIES” - AL-KHWARIZMI 2023**

Muharrir
Musahhih
Texnik muharrir

N.K. Choriyev
O. Sharapova
O. Mirzayev

2023 yil 12-sentyabrda SamDU Tahririy-nashriyot bo‘limiga qabul qilindi.
2023 yil 19-sentyabrda original-maketdan bosishga ruxsat etildi.
Qog‘oz bichimi 60x84. 1/16. “Times New Roman” garniturasini.
Offset qog‘ozini. Shartli bosma tabog‘i - 19,5.
Adadi 50 nusxa. Buyurtma № 594

SamDU Tahririy nashriyot bo‘limida chop etildi.
140104, Samarqand sh., Universitet xiyoboni, 15.

